Radical Addition of Thiophenol to Bicyelo[2.2.2]oct-2ene (III).-Employing a procedure similar to that of Cristol and Brindell, ${ }^{28}$ an equimolar quantity of freshly distilled thiophenol was added to 4.0 g . ( 0.037 mole ) of III. Distillation of the reaction mixture gave $5.53 \mathrm{~g} .(68 \%)$ of $2-$ thiophenylbicyclo [2.2.2]octane, b.p. 118-122 ${ }^{\circ}$ ( 0.8 mm .), $n^{25} \mathrm{D} 1.5859$. A portion of this material was redistilled for analysis, b.p. $113.4-114^{\circ}\left(0.6 \mathrm{~mm}\right.$.) , $n^{23 \mathrm{D}}$ 1.5851. The infrared spectrum (capillary) shows the following bands in the fingerprint region: $1270(\mathrm{~m}), 1200(\mathrm{w}), 1093(\mathrm{~m}), 1067(\mathrm{w})$, $1027(\mathrm{~m}), 961(\mathrm{w}), 742(\mathrm{~s})$ (doublet) and $695(\mathrm{~s})$ (doublet) $\mathrm{cm} .^{-1}$.
(28) S. J. Cristol and G. D. Brindell, J. Am. Chem. Soc., 76, 5699 (1954).

Anal. Calcd. for $\mathrm{C}_{14} \mathrm{H}_{18} \mathrm{~S}: \mathrm{C}, 77.00 ; \mathrm{H}, 8.31 ; \mathrm{S}, 14.69$. Found: C, 77.25 ; H, 8.33 ; S, 14.91 .

Desulfurization of 2-Thiophenylbicyclo[2.2.2]octane.Approximately 5 g . of Raney nickel was added to a solution of the thioether ( 600 mg .. 2.75 mmoles ) in 40 ml . of $95 \%$ ethanol. The mixture was refluxed for 48 hr . The catalyst was removed by filtration and the filtrate was added to 300 ml . of water. This aqueous solution was then extracted with several portions of pentane and the combined extracts were washed with water, dried and concentrated by distillation. Sublimation of the residue afforded 124 mg . ( $41 \%$ ) of bicyclo[2.2.2]octane, m.p. 166-168.5 ${ }^{\circ}$, m.m.p. 166-169 ${ }^{\circ}$.

The infrared spectrum of this product shows none of the bands characteristic of bicyclo[3.2.1]octane.

## [Contribution from the Department of Chemistry of the University of Pennsylvania, Philadelphia 4, Penna.]

# The Conformations of Substituted Cyclopentanes. II. Maximally Puckered Envelope and Half-chair Models for Fused Ring Systems ${ }^{1}$ 

By Frederick V. Brutcher, Jr., and William Bauer, Jr. ${ }^{2}$<br>Received August 30, 1961

A pair of maximally puckered envelope and half-chair models ( $\theta=60^{\circ}$ ) for use in the description of conformations of highly substituted and ring fused cyclopentanes is presented. Their bond bending energies ( $V_{\mathrm{B}}$ ), torsional energies ( $V_{\mathrm{t}}$ ) and electron correlation energies (London forces, $E_{0}$ ) have been calculated for comparison purposes. The use of these models in the estimation of the relative stabilities of the envelope and half-chair conformation of given molecules is discussed.

In a previous paper, ${ }^{3}$ the two important conformations, the envelope (I) and half-chair (II) were described and applied to simply substituted, monocyclic cyclopentanes. In order to utilize these conformations in fused ring systems, however, models must be constructed in which the projected angle, $\theta_{1,2}$, sighted along $C_{1}-C_{2}$ in I or $\theta_{3,4}$ in II will be $60^{\circ}{ }^{4-6}$ The Pitzer and Donath model for cyclopentane itself has $\theta_{1.2}=\theta_{5,1}=46.1^{\circ}$ for the envelope conformation and $\theta_{3,4}=48.1^{\circ}$ for the half-chair. ${ }^{4}$ Further, our earlier model for cyclopentanone was mainly concerned with the projected angle between the carbonyl group and the $\alpha$-substituent. ${ }^{3}$ In this paper, we have constructed through vector analytical techniques ${ }^{4,7.8}$ a pair of maximally puckered models of general applicability to fused rings and highly substituted cyclopentanes.

We begin with a planar, five-membered ring located in a coördinate system as shown below

[^0]

I

(III). The amplitude of puckering $(q)^{4,9}$ was allowed to increase until the torsional angles ( $\theta$ 's)

had in each form reached the desired values. The interior angles of the ring ( $\omega_{i}$ ) and torsional angles ( $\theta_{\mathrm{ij}}$ ) for the resulting, symmetrical models are given in Table I. ${ }^{10}$

[^1]| Angle | $(\mathrm{e} \stackrel{\text { Envelope }}{0.633} \mathrm{~A} .)$ |  |
| :---: | :---: | :---: |
| $\omega_{1}=\omega_{2}=\omega_{5}$ | $96.6{ }^{\circ}$ | $103.0^{\circ}$ |
| $\omega_{3}=\omega_{4}$ | $104.3{ }^{\circ}$ | $95.9^{\circ}$ |
| $\theta_{1,2}=\theta_{5,1}$ | $60.0{ }^{\circ}$ | $19.0{ }^{\circ}$ |
| $\theta_{2,3}=\theta_{4,5}$ | $36.5{ }^{\circ}$ | $50.0{ }^{\circ}$ |
| $\theta_{3.4}$ | $0.0^{\circ}$ | $60.0^{\circ}$ |

It is interesting to observe that while the envelope has two fully staggered ethanes as compared to the one possessed by the half-chair, its remaining positions are relatively more eclipsed than those of the half-chair with the net result that the total torsional energies are essentially identical (see Table II). Further, it is of prime interest to call attention to the intriguing strain energy distribution about the cyclopentane ring. It is apparent that any carbon atom of the ring whose $\mathrm{C}-\mathrm{H}$ bonds are under intense torsional stress is at the same time a region of least bond-bending deformation. Thus in the envelope, the interior angle of carbon $1, \omega_{1}$, is highly deformed ( $96.6^{\circ}$ ), but carbon 1 has a staggered arrangement of its remaining valence bonds. In the envelope, carbon 3 has a high torsion energy with one eclipsed and one partially eclipsed ethane-like interaction, but it has a minimal stress due to bond-bending ( $\omega_{3}=$ $104.3^{\circ}$ ). The same considerations apply to the half-chair and lead one to conclude that the strain energy of puckering in cyclopentane is not borne too unequally by any one carbon atom in the ring, but rather is well distributed around the entire system. It is this smooth distribution that permits pseudorotation and the destruction of such distribution on substitution that allows one or the other of these conformations to be favored in cyclopentane derivatives.

Table II

| Energies of the Maximally Puckered | Cyclopentanes |  |
| :--- | :---: | :---: |
| Energy contribution | Envelope | Half-chair |
| Bond bending $V_{\mathrm{B}}$ | 9.68 | 8.69 |
| Torsion $V_{\mathrm{t}}$ | 4.66 | 4.70 |
| Zero point vibration | 85.26 | 85.26 |
| Electron correlation $\left(E_{\mathrm{c}}\right)$ | -47.95 | -47.29 |
| Bond formation | -59.0 | -59.0 |
| Heat of formation $H_{0}{ }^{0}$ | -7.35 | -7.64 |
| $H_{0}{ }^{\circ}$ at $q=0.5^{a}$ | -9.02 | $\left(q 0.48^{a}\right)$ |

${ }^{a}$ The heats of formation of cyclopentane itself, as given by Pitzer and Donath.

It is now necessary to employ the above models in detailed calculations of their energy content. It is apparent that where appropriate force constants ( $k$ ) for bond bending and potential barriers to rotation ( $V_{0}$ ) are available from simpler systems, one can estimate the bond bending ( $V_{B}$ ) and torsional energies ( $V_{\mathrm{T}}$ ) of the possible conformations of a given molecule from the standard eq. i and ii. The values for $\omega_{0}$ are here taken as $109.5^{\circ}$ and $116.3^{\circ}$ (CCC bond angles in acetone) ${ }^{11}$ for tetrahedral

$$
\begin{align*}
V_{\mathrm{B}} & =k / 2\left(\omega_{0}-\omega\right)^{2} \\
V_{\mathrm{T}} & =V_{0} / 2\left(1+\cos 3 \theta_{i j}\right) \tag{ii}
\end{align*}
$$

and trigonal carbon, respectively. The ethane
(11) P. von R. Schleyer and R. D. Nicholas, J. Am. Chem. Soc., 83, 182 (1961), and references quoted therein.
potential barrier $V_{0}=2.800 \mathrm{kcal} . /$ mole and a bondbending force constant ${ }^{12}$ of $k / 2=0.0175 \mathrm{kcal}$./ mole were employed to give the strain energies of the maximally puckered models. Thus the total energy required to deform the interior angles of the ring in the envelope form is

```
\(V_{\mathrm{B}}=0.0175\left(3\left(109.5-\omega_{1}\right)^{2}+2\left(109.5-\omega_{3}\right)^{2}\right)\)
    \(=3(2.912)+2(0.473)=9.68 \mathrm{kcal} . / \mathrm{mole}\)
```

as there are three angles with the magnitude of $\omega_{1}$ and two with that of $\omega_{3}$. And, the total torsional strain energy of the half-chair is

$$
\begin{aligned}
V_{t}= & 1.400(2(1+\cos 3 \times 19.0)+2(1+\cos 3 \times 50.0) \\
& +(1+\cos 3 \times 60.0)) \\
= & 1.400(2 \times 1.545+2 \times 0.134+0.000) \\
= & 4.326+0.376=4.70 \mathrm{kcal} . / \mathrm{mole}
\end{aligned}
$$

as there are two angles of $19.0^{\circ}$, two of $50.0^{\circ}$ and one of $60.0^{\circ}$ in this model.

However the above considerations are not enough. It is necessary to include the electron correlation energies (London or dispersion energies) in accord with Pitzer's significant discovery ${ }^{4}$ that inclusion of this energy leads ultimately to reasonably good heats of formation of cyclic hydrocarbons. The zero point vibrational energy and heat of bond formation given by Pitzer and Donath in their work are retained.

While the data in Table II will be utilized in detail in a companion paper and later reports, it does help to illuminate a question we had wondered about earlier. We had found that cyclopentane and cyclohexane compounds behaved similarly toward four-center type reactions. ${ }^{3}$ These reactions are of the type where maximum speed is obtained by coplanarity of the four centers of importance. Table II helps explain why the two rings might behave similarly. A simple monosubstituted ring such as cyclopentyl chloride would according to our present estimates be puckered about as much as cyclopentane itself. If the ring is in the envelope conformation and at least some of the chloride is axial, then trans-hydrogens will not be quite coplanar with the chlorine for easy $\mathrm{E}_{2}$ elimination. However, the cost of puckering the ring a bit further if this is required such that the trans diaxial groups are now coplanar is about $0.02-7.35=1.67 \mathrm{kcal}$. The range for the halfchair is $8.49-7.64=0.85 \mathrm{kcal}$. It is therefore apparent that the range of energy differences is sufficiently small so that the cyclopentane ring can compete successfully with the cyclohexane ring toward four-center reactions.

At the equilibrium position for cyclopentane itself, Pitzer and Donath found that the envelope was slightly more stable than the half-chair by 0.53 kcal. ${ }^{4}$ We find in the maximally puckered models in Table II that the electron correlation value for the envelope is again less than for the halfchair, but the effect is partially wiped out in the

[^2]envelope by the rapid increase of bond bending strain so that the two heats of formation, 7.35 vs. 7.64 kcal. , are nearly equal.

It is important to note that the treatment above does not include calculations of repulsive van der Waals forces. They are not operative in these simple models since the closest approach of $2,5-$ diaxial protons in the envelope is $2.22 \AA$., a separation which is greater of 2,5 -diaxial protons in the envelope is $2.22 \AA$., a separation which is greater than their collision diameter.

On substitution it will often prove the case that some internuclear distances will give rise to considerable van der Waal's repulsion. In order that these repulsions can be estimated, the coördinates of the ring atoms and unit vectors for substituents are given in Table III.

Table III

| Envelope model (VI) |  |  |  | Half chair model (III) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Coordinates of the carbon nuclei coobrdinate |  |  |  | Coördinates of the carbon nuclei coördinate |  |  |  |
| Atom | + | , | - | Atom | - | - | $z$ |
| 1 | 0.000 | 0.000 | 0.400 | 1 | 0.000 | 0.000 | 0.000 |
| 2 | 0.725 | 1.150 | . 324 | 2 | 0.959 | 1.183 | . 229 |
| 3 | 2.148 | 0.770 | 124 | 3 | 2.283 | 0.675 | 370 |
| 4 | 2.148 | -0.770 | 124 | 4 | 2.283 | -0.675 | 70 |
| 5 | 0.725 | $-1.150$ | . 324 | 5 | 0.959 | $-1.183$ | 229 |
| Unit vectors for tetrahedral substituents |  |  |  | Unit vectors for tetrahedral substituents |  |  |  |
| $1 \mathrm{H}^{\text {a }}$ | . 169 | 0.000 | . 98 | 1u | -0.576 | 0.155 | 0.802 |
| $1 d^{\text {b }}$ | . 986 | . 000 | . 168 | 1 d | . 576 | -. 155 | 802 |
| 2 u | . 280 | . 900 | . 332 | 24 | -. 319 | . 822 | 476 |
| 2d | . 114 | . 039 | . 992 | 2d | . 099 | . 202 | 975 |
| 3 u | 190 | . 354 | . 915 | 3 u | -. 050 | . 103 | . 994 |
| 3d | . 679 | . 354 | -. 642 | 3d | . 780 | . 575 | 244 |
| 4 u | 190 | 354 | . 915 | 4 | . 780 | . 575 | 244 |
| 4 d | . 679 | . 354 | . 642 | 4 | $-.050$ | 103 | 994 |
| 5 u | $-.280$ | -. 900 | . 33 | 5 | . 099 | . 202 | 975 |
| 5 d | $-.1$ | . 039 | -. 9 | 5 | -. 319 | . 882 | 476 |
| Unit vectors for trigonal bonding |  |  |  | Unit vectors for trigonal bonding |  |  |  |
| $1 t^{\text {c }}$ | -0.708 | 0.000 | 0.707 | 1 t | -1.000 | 0.000 | 0.000 |
| 2t | $-.341$ | . 746 | -. 572 | 2 t | $-0.191$ | . 887 | -. 432 |
| 3 t | . 753 | . 614 | . 237 | 3 t | . 642 | . 409 | . 649 |
| 4 t | . 753 | . 614 | . 237 | 4 t | . 642 | . 409 | -. 649 |
| 5 t | . 341 | -. 746 | -. 572 | 5 t | -. 191 | -. 887 | . 432 |

a Where $u$ means up. ${ }^{b}$ Where $d$ means down. © Where $t$ means trigonal.

Internuclear Distances.-The beginning of the unit vector $5 \mathrm{~d}(V)$ is located at $C_{5}$ 's, $x, y, z$ coordinates. How does one obtain the coördinates of 5 d 's terminus? This is done by using $\mathrm{C}_{6}$ 's $x, y, z$ coördinates and adding or subtracting the corresponding $x, y, z$ values for 5 d given in Table III. This has the effect of a movement from $\mathrm{C}_{5}$ along 5 d to its terminus.


The reason for doing it this way is that the $x, y, z$ values in Table III for $1 \mathrm{u}, 1 \mathrm{~d}, 2 \mathrm{u}$, etc., are set up to be a measure of the distance of each terminus from the parent carbon atom based on a
unit vector (unit movement). Therefore if 5 d were assumed to be an axial carbon atom attached to $C_{5}$ it would be longer ( $1.54 \AA$.) than unity, hence each $x, y, z$ value for 5 d in Table III must be multiplied by 1.54 before addition or subtraction to $\mathrm{C}_{\mathrm{b}}$ 's $x, y, z$ coördinates. These new coördinates, $x$ (0.549), $y(-1.090)$ and $z(-1.852)$ are now those of an axial carbon atom on $\mathrm{C}_{5}$ such as might be the case for an axial methyl group. It might be pointed out that in the example below, $i, j$ and $k$ are unit vectors along the $x, y, z$ axes, respectively

$$
\begin{aligned}
1.54 \times 5 \mathrm{~d} & =1.54(-0.114 i-0.039 j-0.992 k) \\
& =-0.176 i-0.060 j-1.528 k \\
\mathrm{C}_{6} & =\frac{0.725 i-1.150 j-0.324 k}{0.549 i-1.090 j-1.852 k}
\end{aligned}
$$

Similarly for the 2 d proton on $\mathrm{C}_{2}$ its coördinates (for $\mathrm{C}-\mathrm{H}$ equal to $1.10 \AA$.) turn out to be $0.600 i+$ $1.107 j-1.415 k$. Now to obtain the internuclear distance between the $\mathrm{CH}_{3}$ and $\mathrm{C}_{2}$ proton one takes the square root of the sum of the squares of the differences in like coördinates which in this case turns out to be $2.24 \AA$.
$\mathrm{CH}_{3}, \mathrm{H}$ distance $=2.24=\left[(0.600-0.549)^{2}+(1.107+\right.$

$$
\left.1.090)^{2}+(-1.415+1.852)^{2}\right]^{1 / 2}
$$

This is well within the sum of the van der Waals radii of these two groups and corresponds to considerable repulsive energy. Since structure V above is analogous upon rotation to VI, a possible conformation of a steroid ring $D$, we have, in principle, by the method outlined above analyzed the $\mathrm{C}_{13}$ methyl- $\mathrm{C}_{15}$ hydrogen interaction in a C/D trans fused steroid.

Dipole Moments.-The unit vectors of Table III also present a convenient method of calculating the dipole moments of cyclopentane systems. Thus we may wish to consider the dipole moments of the $16 \alpha$-bromo- 17 -ketosteroids which have been assigned the envelope conformation (VII) on the basis of spectral data. ${ }^{1,13}$ Bond moments for the carbonyl group and the carbon-bromine bond are taken as 2.91 and 2.10 D., respectively, in accord with the observed moments of the chloro- and bromocamphors. ${ }^{3,14}$ Here the appropriate unit vectors are treated as having unit dipole moment; hence each must be multiplied by the appropriate total moment for each group.

Further the $U_{\mathrm{C}}-\mathrm{o}$ involves a trigonal carbon atom; hence $4 t$ of the envelope must be used for this group. Using the unit vector $3 u$ for $\mathrm{C}-\mathrm{Br}$ and $4 t$ for $\mathrm{C}=0$ there is obtained

$$
\begin{aligned}
& u_{\mathrm{O}-\mathrm{Br}}=2.10(0.190 i+0.354 j+0.915 k)=0.399 i+ \\
& 0.743 j+1.922 k \\
& u_{\mathrm{C}-\mathrm{O}}=2.91(0.753 i-0.614 j+0.237 k)=2.191 i- \\
& 1.787 j+0.690 k
\end{aligned}
$$

The vector sum of the bond moments, $u \mathrm{C}-\mathrm{Br}+$ $u_{\mathrm{c}=0}=u_{\text {total }}$, gives the coördinates of the molecules total moment, $u_{\text {total }}=2.590 i-1.044 j+$ $2.612 k$. Then $u^{2}=(2.5901)^{2}+(-1.044)^{2}+$
(13) J. Fishman and C. Djerassi, F.xperientia, 15, 138 (1960): J. Fishman, J. Am. Chem. Soc., 82, 6143 (1960).
(14) W. D. Kumier, N. Pearson and F. V. Brutcher, Jr., ibid., 83, 2711 (1961).
$(2.612)^{2}$ gives the magnitude of the moment (3.82 D.). This value is in excellent agreement with the observed moment of $16 \alpha$-bromo- $5 \alpha$ -
androstan-17-one which we have measured in benzene solution at $25^{\circ}$ and found to be $3.85 \mathrm{D} .{ }^{15}$
(15) Unpublished data of F. V. Brutcher, Jr., and F. J. Reynolds.
[Contribution from the Department of Chemistry of the University of Pennsylvania, Philadelphia 4, Penva.]

# The Conformations of Substituted Cyclopentanes. III. Ring D in the Steroids ${ }^{1,2}$ 

By Frederick V. Brutcher, Jr., and William Bauer, Jr. Received August 30, 1961


#### Abstract

The previously-described, ${ }^{1}$ maximally-puckered models for the symmetrical forms of cyclopentane have been applied to the description of three possible conformations of ring D in the steroids. Calculation of bond-bending and torsional energies as well as interaction energies for 1,3 -substituents has suggested general stability relationships for these conformations on substitution of the ring. Infrared data on steroid haloketones and glycols have been utilized in assignment of conformation to several steroids. Some of the chemistry of ring $D$ is discussed in the light of the conformations of the ring.


The most famous relative of the simple cyclopentane ring is certainly the five-membered ring $D$ of the steroids. ${ }^{3-7}$ In a previous paper we have constructed by vector analytical techniques ${ }^{1,8}$ models of maximally puckered cyclopentane rings such as would be found in the trans-locked C/D ring system. In this paper we apply these models to ring D and interpret some of its chemistry.

As a first step, the three symmetrical conformations of ring $D$ were constructed (I, II, III). Conformations I and II have been previously recorded in the literature while III has been hitherto neglected. Envelope conformation $I^{2}$ is that which has earlier been generally used by chemists having had its birth in Barton's original drawing of the steroid molecule. ${ }^{9}$ Envelope I has $\mathrm{C}_{14}$ below the plane of $\mathrm{C}_{13}, \mathrm{C}_{15}, \mathrm{C}_{16}, \mathrm{C}_{17}$. Half-chair II is an arrangement which has been discussed in detail for simple cyclopentanes ${ }^{2}$; it has $\mathrm{C}_{13}$ above and $\mathrm{C}_{14}$ an equal distance below the $\mathrm{C}_{15}, \mathrm{C}_{16}, \mathrm{C}_{17}$ plane. Finally there is the previously neglected envelope III. This last conformation has $\mathrm{C}_{14}, \mathrm{C}_{15}, \mathrm{C}_{16}$ and $\mathrm{C}_{17}$ in a single plane while $\mathrm{C}_{13}$ lies above the plane. ${ }^{10}$
(1) Paper II, F. V. Brutcher, Jr., and W. Bauer, Jr., J. Am. Chem. Soc., 82. 2233 (1962); see also F. V. Brutcher, Jr., and W. Batuer, Jr., Science, 132, 1489 (1960).
(2) F. V. Brutcher, Jr., T. Roberts, S. J. Barr and N. Pearson, J. Am. Chem. Soc., 81, 4915 (1959).
(3) See L. F. Fieser and M. Fieser, ''Steroids," Reinhold Publishing Corp., New York, N. Y., 1959.
(4) Eliel and Pillar ${ }^{5}$ as well as Dauben and Pitzer ${ }^{6}$ have considered the distortion in a cyclohexane ring arising upon fusion to a cyclopentane ring. They conclude that in the trans isomer the distortion is toward a more severe chair conformation. In hydrindane this causes crowding of the axial hydrogen atoms. When one of these is replaced by a methyl group as in the steroids, distortion of the cyclohexane ring in this fashion is, hence. exceedingly costly energywise and one expects it to be at a minimum. Eliel has presented experimental data which verify the existence of these distortions and at the same time indicate that they are, indeed, small. ${ }^{5}$ With regard to the five-mem. bered ring in the hydrindanes, Allinger and Coke ( $J$. Am. Chem. Soc., 82. 2553 (1960)) have found that the cis isomer has a larger entropy and point out that this may be due to a larger partial pseudorotation (cf. J. P. McCullough, J. Chem. Phys., 29, 966 (1958)) in the cis isomer.
(5) E. L. Eliel and C. Pillar, J. Am. Chem. Soc., 77, 3600 (1955).
(6) W. G. Dauben and K. S. Pitzer in M. S. Newman, "Steric Effects in Organic Chemistry," J. Wiley and Sons, Inc., New York, N. Y., 1956, p. 37.
(7) For a discussion of several steroidal hydrindanones, see Fieser and Fieser, ref. 3, page 211 ff .
(8) K. S. Pitzer and W. N. Donath, J. Am. Chem. Soc., 81, 3213 (1959).
(9) D. H. R. Barton, J. Chem. Soc., 1027 (1953).
(10) These three conformations may be considered to arise through a partial pseudorotation, the ring fusion preventing the full pseudorota. tion cycie from taking place.


The next step in our analysis was to compare these three conformations with regard to their torsional $\left(V_{\mathrm{t}}\right)$ and angle-strain $\left(V_{\mathrm{B}}\right)$ energies, their electron-correlation energies ( $E_{\mathrm{c}}$ ) (London or dispersion energies) and any significant 1,3 -interactions of a repulsive nature (van der Waals repulsive forces). In view of the laborious mathematical operation of summing up all $\mathrm{C}-\mathrm{C}, \mathrm{C}-\mathrm{H}$ and $\mathrm{H}-\mathrm{H}$ non-bonded London interactions, it was convenient to assume that the London force difference between envelope I (or III) and half-chair II is essentially the same as in the parent, unsubstituted, maxi-mally-puckered models. Here ${ }^{1}$ the envelope ( $E_{c}$ $-47.95 \mathrm{kcal} . /$ mole) is stabilized $0.66 \mathrm{kcal} . /$ mole more than the half-chair ( $E_{\mathrm{c}}-47.29 \mathrm{kcal} . / \mathrm{mole}$ ) or, in other words, the half-chair has 0.66 kcal ./ mole more energy than the envelope due to the London force effect. We therefore add 0.66 $\mathrm{kcal} . /$ mole to the half-chair II when bond-bonding and torsional energies are being calculated.

For cases where interior angle strain energy and also correlation energy can be taken to be the same as in the parent conformations a new correction factor of $0.33 \mathrm{kcal} . / \mathrm{mole}$ is of use. Substitutions of the type such as methyl, halogen or hydroxyl which change only the torsional energy would lead to this situation. This correction factor is derived by noting that the difference in bond-bending energies between the envelope ( $9.68 \mathrm{kcal} . /$ mole) and the half-chair ( $8.69 \mathrm{kcal} . /$ mole) favors the half-chair by $0.99 \mathrm{kcal} . /$ mole When this quantity is combined with the correlation energy difference ( $-0.66 \mathrm{kcal} . /$ mole) one arrives at the factor 0.33 kcal./mole favoring the half-chair; this energy is then added to envelope conformations I and III.

Another important factor does exist. In addition to the above energy terms the axial methyl group on $\mathrm{C}_{13}$ has the potentiality of strong inter action of repulsive, van der Waals type with the hydrogens at $\mathrm{C}_{15}$ and $\mathrm{C}_{16}$. The earlier calculations for our unsubstituted medels did not require int


[^0]:    (1) Previous communication in this series, F. V. Brutcher, Jr., and William Bauer, Jr., Science, 132, 1489 (1960). The material in this paper and the following one on ring $D$ in the steroids was presented at the Autumn Meeting of the National Academy of Sciences held at the University of Pennsylvania on November 14, 1960.
    (2) Armstrong Cork Co. Predoctoral Fellow 1960-1961.
    (3) F. V. Brutcher, Jr., T. Roberts, S. J. Barr and N. Pearson, J. Am. Chem. Soc., 81, 4915 (1959).
    (4) K. S. Pitzer and W. E. Donath, ibid., 81, 3213 (1959).
    (5) Inspection of scale models of steroid rings $C$ and $D$ built according to the reported X•ray analyses of several steroid systemsi ndir cates that this is approximately the case. ${ }^{6}$ The much more complicated fused ring cases, where $\theta$ may not be equal to $60^{\circ}$, are under consideration in this Laboratory.
    (6) (a) C. H. Carlisle and D. Crowfoot, Proc. Royal Soc. (London), 1844, 81 (1945) ; (b) D. Crowfoot, Hodgkin and D. Sayre, J. Chem. Soc., 4561 (1952); (c) R. G. Curtis, J. Friedrichsons and A. McL. Mathieson, Nautre, 170, 321 (1952); J. Chem. Soc., 2159 (1953).
    (7) The treatment involves the assumption that the angles $\omega_{2}=$ $\omega_{5}$ are also equal to $\omega_{1}$. This assumption, which makes the calculations tractable; was found by Rilpatrick, Pitzer and Spitzers to give substantially the lowest energy.
    (8) J. E. Kilpatrick, K. S. Pitzer and R. Spitzer, J. Am. Chem. Soc., 60, 211 (1947).

[^1]:    (9) It is important to note that $q$ in $\AA$., which is a measure of the amplitude of puckering, is not the distance of carbon 1 in the envelope out of the $\mathrm{C}_{2}-\mathrm{C}_{5}-\mathrm{C}_{4}-\mathrm{C}_{5}$ plane. We have transformed $q$ for cyclopentane itself and also for our maximally puckered models to the following numbers which are more meaningful for organic chemists. In cyclopentane itself the $\mathrm{C}_{1}$ distance (envelope) from the $\mathrm{C}_{2}-\mathrm{C}_{8}-\mathrm{C}_{4}-\mathrm{C}_{6}$ plane is $0.75 \AA$; in our maximally puckered model it is $0.91 \AA$. For the half-chair with $\mathrm{C}_{7}-\mathrm{C}_{1}-\mathrm{C}_{6}$ the reference plane, $\mathrm{C}_{3}$ in cyclopentane itself is $0.38 \AA$. above the reference plane while $\mathrm{C}_{4}$ is equally below the plane. In our maximally puckered model (half-chair) $C_{3}$ is $0.48 \AA$. above and $\mathrm{C}_{4}$ is $0.48 \AA$. below the $\mathrm{C}_{2}-\mathrm{C}_{1}-\mathrm{C}_{5}$ plane. It also might be pointed out that $q$ is not needed for vector analytical work on organic molecules (e.g., for cyclohexene see E. J. Corey and R. A. Sneen, ibid., 77, 2505 (1954) and for bicycloheptane, C. F. Wilcox, ibid., 82, 414 (1960)). The technicque involving $q$ is derived from vibrational methods of analysis such as those used for pseudorotating molecules such as cyclopentane, ${ }^{8}$
    (10) It is useful to note that when a cyclopentane ring adopts either the envelope or half-chair all interior angles turn out to be less than the tetrahedral value of $109^{\circ} 28^{\prime}$.

[^2]:    (12) The available information on force constants for deforming certain $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angles is disappointingly limited. For example, the force constant for deforming the $116.3^{\circ} \mathrm{C}-\mathrm{C}-\mathrm{C}$ angle of acetone or other simple ketones is unknown and must be estimated. For a scholarly discussion of force constants and related material see West. heimer's chapter in M. S. Newman, "Steric Effects in Organic Chemistry," J. Wiley and Sons, Inc., New York, N. Y., 1958, Chapt. 1.

